

# Modelling and control summaries



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## Nyquist 7: Self-study tutorial sheet

This is primarily for students to practise. Attempt questions by hand and only after completion, use MATLAB to test your solutions.

### QUESTION 1. Sketch Nyquist of the following

$$G = \frac{4}{s(s+5)}; \quad H = \frac{10(s+2)}{(s+5)^2};$$

$$N = \frac{0.0005(s+0.02)}{(0.008-s)(0.06+s)}$$

$$M = \frac{2(s+10)}{s(s+1)(s+4)}; \quad P = \frac{3}{(s-1)(s+6)}$$

$$L = \frac{s+2}{s^2(s+4)}$$

G=tf(4,[1 5 0]);  
H=tf([10 20],[1 10 25])  
M=tf([2 20],poly([0 -1 -4]))

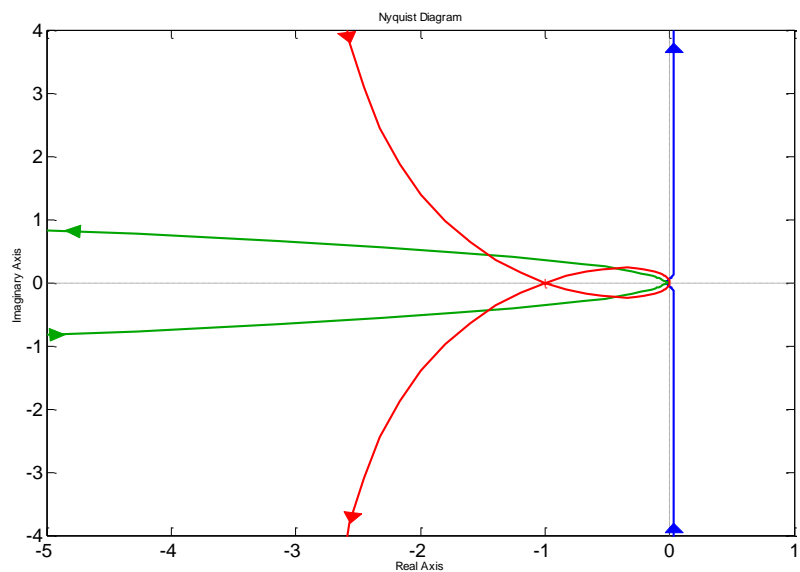
P=tf(3,poly([1 -6]))  
N=tf(0.0005\*[1 0.02],poly([0.008,-0.06])\*(-1))  
L=tf([1 2],[1 4 0 0])

### QUESTION 2. Match systems to the Nyquist plots

$$G1 = \frac{s+1}{s(s+4)(s+3)}$$

$$G2 = \frac{s+1}{s^2(s+4)}$$

$$G3 = \frac{s+2}{s(s-1)}$$



### Sketch the Bode/Nyquist diagrams with and without compensation

$$G(s) = \frac{0.3(s+10)}{s(s+1)(s+2)}; \quad K_1(s) = 2 \frac{s+0.5}{s+2}$$

$$G(s) = \frac{0.4(s+5)}{s(s+0.5)(s+2)}; \quad K_1(s) = 0.5;$$

$$G(s) = \frac{6(s+1)}{s(s-1)(s+3)}; \quad K_1 = \frac{4(s+2)}{s+5}; \quad K_2 = \frac{4(s+0.1)}{(s+0.04)}$$

$$K_2(s) = \frac{2(s+0.05)}{(s+0.2)}; \quad K_3(s) = \frac{2(s+0.5)}{(s+2)}$$

$$G(s) = \frac{0.001(s+4)}{s(s+0.1)^2(s+2)}; \quad K_1(s) = 2 \frac{s+0.06}{s+0.18}; \quad K_2 = \frac{1}{3} \left( \frac{s+0.18}{s+0.006} \right)$$

$$G(s) = \frac{10(s+1)}{s(s+4)(s-2)}; \quad K = 4; \quad K_1(s) = 8 \frac{s+3}{s+12}; \quad K_2 = \frac{s+12}{s+3}$$

$$G(s) = \frac{4-4s}{s(s+2)(s+3)}; \quad K_1(s) = 1; \quad K_2(s) = 0.5; \quad K_3(s) = 0.25 \frac{(s+0.1)}{(s+0.05)}$$

You can overlay Bode/Nyquist plots on MATLAB as follows

```
>> nyquist(G,G*K1,G*K2);legend('G','GK1','GK2')
```

By computing the initial quadrant carefully, sketch Nyquist diagrams of the following.

$$G_1(s) = \frac{4.5s+3}{s^2(s+1)(s+2)}; \quad G_2(s) = \frac{6s+3}{s^2(s+1)(s+2)}; \quad G_3(s) = \frac{2s+3}{s^2(s+1)(s+2)}$$

$$G(s) = \frac{s+10}{(s+1)(s+2)}$$

Give an explanation of how dead-time affects Bode and Nyquist diagrams. Illustrate with several examples.