

# Modelling and control summaries



by Anthony Rossiter

## Intro. to feedback 3 – implementation

**FEEDBACK INVOLVES MEASUREMENT, DECISION MAKING BASED ON THE MEASUREMENT AND INPUT ADJUSTMENT.**

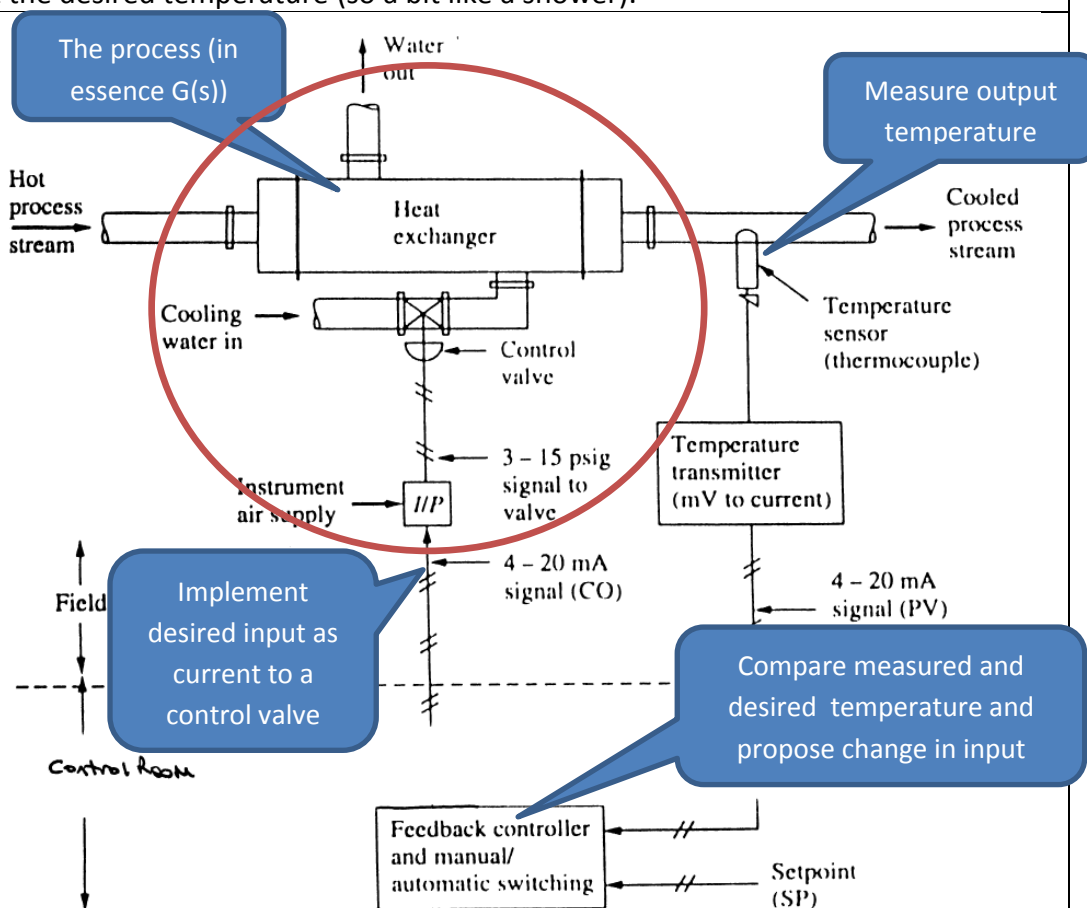
In order to design this effectively, we need a systematic framework for analysing the process.

**Heat exchanger:** this is a very common component within industry. The aim is to ensure the output stream is at the desired temperature (so a bit like a shower).

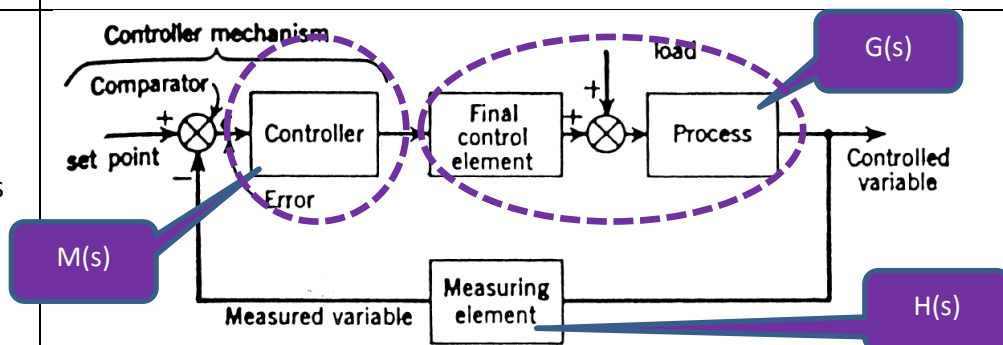
This diagram is useful as it shows the key processes involved in feedback.

- i) measurement
- ii) decision making.
- iii) implement input  $u(t)$ .
- iv) process dynamics.

Output depends through the process dynamics on the selected input.



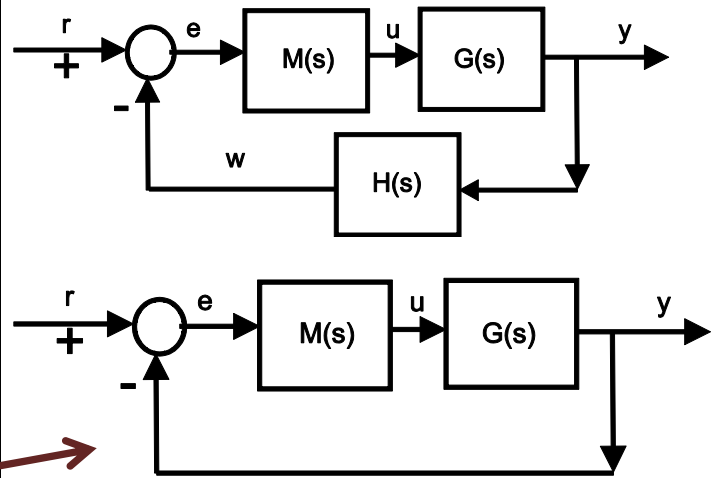
We use an equivalent block diagram to simplify analysis as this is far easier to work with.



**SUMMARY** – we can reduce the implementation to a simple block diagram with 3 key blocks and a comparator. Note any valve dynamics are considered part of the process.

1.  $G(s)$  represents process dynamics between the input  $u(t)$  and output  $y(t)$ .
2.  $u(t)$  is the result of the decision making.
3. Decision making is captured in  $M(s)$  and typically uses the error between the measured output  $w$  and the target  $r$ , that is  $e=r-w$ .
4.  $w(t)$  is the measured output from sensor  $H(s)$  – true output  $y(t)$  is of course unknown.

**CAVIAT:** It is common to assume  $H(s) \approx 1$ , that is sensing is instantaneous and accurate. Hence simplify diagram to:



**COMPARING OPEN-LOOP AND CLOSED-LOOP:** Detailed analysis of block diagrams is in the chapter on block diagrams. Here the equations are assumed. Let  $R(s)$  be desired target.

OPEN- LOOP ( $N(s)$  to be chosen)

$$Y(s) = G(s)U(s) = G(s)N(s)R(s)$$

CLOSED- LOOP ( $M(s)$  to be chosen)

$$Y(s) = \frac{G(s)M(s)}{1 + G(s)M(s)} R(s) = G_c(s)R(s)$$

**KEY OBSERVATIONS:**

1. The transfer function between the target  $R(s)$  and the output  $Y(s)$  is very different in open-loop and closed-loop.
2. This means that the closed-loop and open-loop will have different poles, different steady-state gains and different behaviour.
3. We know that it is impossible to design  $N(s)$  to give good open-loop control in general due to uncertainty in modelling  $G(s)$ .
4. The challenge is to design an effective control law  $M(s)$  so that the behaviour of  $G_c(s)$  is good, notwithstanding any errors in the model assumed for  $G(s)$ .

The challenge for students is to undertake the analysis of  $G_c(s)$  and determine effective mechanisms for selecting  $M(s)$  so that  $G_c(s)$  has the desired behaviour.

**REMINDER:** An automated feedback system requires four main components:

1. A sensor to observe the output.
2. A comparator to compare the output with the target.
3. An intelligent component to decide what the new input should be. [In practice the comparator is embedded within this.]
4. An actuator, or similar, to implement the desired input.